# **R** Functions

Things Your Mother (Probably) Didn't Tell You About

## **R** and Extensibility

- The success that R currently enjoys is largely because the environment is *extensible*.
  - Developers can easily add new capabilities.
  - Users can quickly develop and customise their own methodology.
- Both developers and users implement their extensions in the same way as new R functions.
- This uniform method of extension provides a certain unity to the process of R development and it is natural to move from being a user to being a developer.

## What Is An R Function?

- An R function is a packaged recipe that converts one or more inputs (called arguments) into a single output.
- The recipe is implemented as a single R expression that uses the values of the arguments to compute the result.
- Functions are first-class values. They can be:
  - assigned as values of variables
  - passed as arguments to other functions

# An Example

• The following function takes a single input value and computes its square.

> square = function(x) x \* x

- The function is created and then assigned the name square.
- The variable, x, is a *formal parameter* of the function.
- When the function is *called* it is passed an *argument* that provides a value for the formal parameter.

> square(1:5)
[1] 1 4 9 16 25

# **Combining Functions**

• Functions defined by users are identical in nature to those provided by the system and can be used in exactly the same way.

```
> sum(1:10)
[1] 55
```

```
> sum.of.squares =
    function(x)
    sum(square(x))
```

```
> sum.of.squares(1:10)
[1] 385
```

# **Optional Arguments**

- R functions can have many arguments (the default plot function has 16).
- Function definitions can allow arguments to take *default values* so that users do not need to provide values for every argument.
- If the plot function is called with a single argument it is used to provide *y* values for the plot; all other arguments take on default values.
- Default arguments are specified as follows:

```
parameter = expression
```

# Example

- The following variant of sum.of.squares adds a second parameter so that the function returns the sum-of-squares of deviations about the second value.
- The second argument has a default value equal to the mean of the first.

> sum.of.squares =
 function(x, about = mean(x))
 sum(square(x - about))

• Note that the default argument value is defined in terms of variables internal to the function.

• Since many arguments can take default values, it is useful to have a way of specifying which arguments do not.

```
> sum.of.squares(1:10)
[1] 82.5
> sum.of.squares(1:10, about = 0)
[1] 385
```

• There is a set of rules the determine how arguments are matched to parameters.

```
> sum.of.squares(about = 0, 1:10)
[1] 385
```

• The present definition of sum.of.squares does not work when NA values are present.

```
> sum.of.squares(c(-1, 1, NA))
[1] NA
```

- The inclusion of an NA value produces an NA result.
- It may well be that we want NA values ignored to produce the same result as:

```
> sum.of.squares(c(-1, 1))
[1] 2
```

• Let's modify the sum.of.squares function so that it removes any NA values from x.

```
> sum.of.squares =
   function(x, about = mean(x)) {
        x = x[!is.na(x)]
        sum(square(x - about))
   }
```

```
> sum.of.squares(c(-1, 1, NA))
[1] 2
```

• Let's modify the sum.of.squares function so that it removes any NA values from x.

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> sum.of.squares =
    function(x, about = mean(x)) {
        x = x[!is.na(x)]
        sum(square(x - about))
    }
> sum.of.squares(c(-1, 1, NA))
[1] 2
```

• This produces the "right" result, but the fact that it does so is surprising.

# **Lazy Evaluation**

- R function arguments are not evaluated until the value of the argument is needed.
- In the case of the preceding example, the value of about is not required until the expression

```
sum(square(x - about))
```

is evaluated.

• At that point, the NA values have been deleted from x so that the value of mean(x) is not NA.

# Lazy Evaluation and Side Effects

• Because argument evaluation is lazy, it is dangerous to ever carry out assignment (or any operation with a side effect) in an argument to a function.

```
> x = 10
> y = 20
> f((x = 100), (y = 200))
[1] 300
```

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> x = 10
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> f((x = 100), (y = 200))
[1] 300
> x; y
[1] 10
[1] 20
```

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[1] 300
> x; y
[1] 10
[1] 20
```

• This is because the function f is defined as follows.

> f = function(a, b) 300

# Scoping

- The *scoping rules* of a language describe how the values of variables are determined.
- R uses *block-structured scope*, similar to languages like Algol-60 and Pascal and Scheme.
- If a function g is defined within a function g, the variables in f are visible in g, unless they are *shadowed* by a local variable.
- The use of these scoping rules make R a very different language from the earlier S language developed at Bell Laboratories.

# Example

• Consider the following nested function definition.

```
> linmap =
  function(x, a, b, swap = FALSE) {
    transform = function(x) {
        if (swap) b + a * x
            else a + b * x
        }
        transform(x)
    }
```

• Within the function transform, the variable name x refers to the argument of transform while a, b and swap refer to the arguments of the enclosing linmap function.

# **A Simple Function**

• The following function adds the value of the global variable x to its argument.

```
> add.x.to = function(u) x + u
> x = 20
> add.x.to(10)
[1] 30
> x = 30
> add.x.to(10)
```

[1] 40

## **Nested Functions**

• The function add.x.to looks just like the previous one, but now the value of x is an argument to the enclosing function add.

```
> add =
    function(x, y) {
        add.x.to = function(u) x + u
        add.x.to(y)
    }
> add(10, 20)
[1] 30
```

# A Function that Returns a Function

• Now we'll change the example so that instead of returning a numeric value the outer function returns the inner function.

```
> make.add.to =
    function(x) {
        add.x.to = function(u) x + u
        add.x.to
    }
> add.10.to = make.add.to(10)
> add.10.to(100)
[1] 110
```

# Variable Capture and Closures

- In the previous example, the variable x came into existence when the outer function make.add.to was called.
- This variable continues to exist after make.add.to returns because it is required for the value returned by make.add.to to make sense.
- The outer functions local variable x has been *captured* by the function returned as a value.
- The variable x is, in a sense "enclosed" within the function returned by make.add.to.
- Functions that enclose data in this way are called *closures*.

# **Captured Variables are Private**

• Each time make.add.to is called, a new x variable is created.

```
> add.10.to = make.add.to(10)
```

```
> add.20.to = make.add.to(20)
```

```
> add.10.to(100)
[1] 110
> add.20.to(100)
[1] 120
```

• This means that each function returned by make.add.to has its own private x variable.

## **Other Ways of Creating Private Variables**

- The use of nested functions is not the only way to create private variables.
- Here are some alternatives.

```
> add.10.to =
    with(list(x = 10),
        function(u) x + u)
> add.20.to =
    local({
        x = 20
        function(u) x + u
    })
```

#### How This is Useful

- The ability to create closures might seem like a fairly esoteric capability, but it provides a way to directly provide many kinds of object used directly in statistics.
- The mechanism is used in many R functions (e.g. splinefun).
- I'll show just one example: likelihoods.

# Likelihoods

• Here is a function that creates a function that computes the negative log likelihood for a sample of normal observations stored in a vector x.

#### Likelihood-Based Estimation

• Given the negative log likelihood it is easy to obtain parameter estimates and standard errors.

```
> res$convergence
[1] 0
```

```
> res$par
[1] -0.03126232 0.86081820
```

> sqrt(diag(solve(res\$hessian)))
[1] 0.08608182 0.06087361

# **Other Applications**

- Many statistical problems can be attacked using likelihood-based analyses, even when they have a non-standard form.
- Markov chains with their associated transition matrices and current states are naturally modelled as closures.
- Complex software can be written without worrying about "namespace clutter."
- The R package facility is implemented using these ideas.
- The S4 object system is implemented using closures.

# Recursion

- The Devil's DP Dictionary defines recursion as follows: **Recursion** (n). *See Recursion*.
- In computing, a function is recursive if, either directly or indirectly, it can make a call itself.
- The prototypical example of recursion is the factorial function.

```
> factorial =
    function(n)
    if (n == 0) 1 else n * factorial(n - 1)
```

# **Example: Computation Using Recursion**

• In the good old days the following kind of problem would have been found in an introductory statistics course:

There are 8 girls and 4 boys in a class. How many ways can they be arranged in a line so that the boys are separated by at least one girl?

- (These days, questions that require thought lead to bad class reviews and they've been done away with.)
- There is a trivial solution to this problem, but let's assume that we aren't smart enough to spot it.
- Instead, we'll attack the problem using recursion.

#### Formulating the Problem as a Recursion

- First let's generalise to the case of g girls and b boys.
- If the number of arrangements is f(b,g), then we have the following recursion.

$$f(b,g) = g \times f(b,g-1) + b \times g \times f(b-1,g-1)$$

- This recursion comes from considering what happens when we pick either a girl or a boy as our first choice.
- In addition to the basic recursion, we also need ensure that there are termination rules that provide a way of stopping the recursion.

#### **Termination Rules**

• The consideration of special cases gets us a number of termination rules.

ConditionFunction Valueb = 1, g = 0,f(b,g) = 1g < b - 1f(b,g) = 0b = 0f(b,g) = g!

# **A Computational Solution**

```
> f =
function(b, g) {
    if (b == 1 && g == 0) 1
    else if (g < b - 1) 0
    else if (b == 0) factorial(g)
    else g * f(b, g - 1) +
        b * g * f(b - 1, g - 1)
}</pre>
```

> f(4, 8) [1] 121927680

# **A Computational Solution**

```
> f =
      function(b, g) {
          if (b == 1 && g == 0) 1
          else if (g < b - 1) 0
          else if (b == 0) factorial(g)
          else g * f(b, g - 1) +
              b * g * f(b - 1, g - 1)
      }
> f(4. 8)
[1] 121927680
```

> factorial(8) \* prod(9:6)
[1] 121927680

#### **The Number of Function Calls**

- The evaluation of f (4, 8) takes 307 calls to f.
- Of these, 306 are calls by f to itself.