Calf Weight Gain Data

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Executive Summary

The average daily weight gains (ADG) of calves during 3 to 9 months of age for three different breeds were compared. It was found that the ADG of calves is affected both by the ADG the calf's sire and by the ADG of the calf's dam. The impact of the dam's ADG was similar across breeds but the impact of the sire's ADG was clearly different for different breeds. For each increase of 1 unit in the dam's ADG, the predicted ADG of the calf increases by 0.512 units. For each increase of 1 unit in the sire's ADG, the predicted ADG of the calf increases by 0.643 units for breed 1, by 0.151 units for breed 2 and by 0.207 units for breed 3.

If we compare calves across breeds where the sire and dam of each calf have the average values of ADG (for that breed), then the predicted ADG is 2.99 for breed 1, 2.51 for breed 2 and 4.17 for breed 3.

Calf Data

This report considers data that was collected to explore the growth rate of calves. The average daily weight gain (ADG) during 3 to 9 months of age for 3 breed of calves was studied. It was thought that ADG is partly an inherited trait. Thus the ADG of each calf's sire and ADG of each calf's dam (when they were growing during 3 to 9 months of age) were considered as possible covariates. The data consists of the following measurements:

breed: breed of calf, a factor with levels 1, 2 or 3.

adg: average daily weight gain of calf.

sadg: average daily weight gain of calf's sire. dadg: average daily weight gain of calf's dam.

The aim was to identify a suitable regression model for adg using the remaining variables as regressors. This model is then to be used to compare weight gains for different breeds. Figure 1 contains the pairwise scatter plots of the data. From these plots it is evident that adg tends to be highest for breed 3 and lowest for breed 2. There is also clear evidence that adg is related (in a positive manner) to both sadg and dadg.

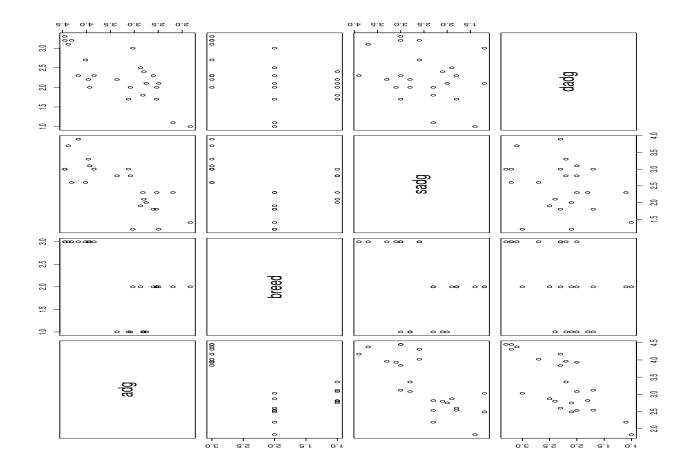


Figure 1: Pairwise Scatterplots of Car Data.

1 Modelling "Average Daily Gain" of Calves

My analysis of the calf data indicated that both sadg and dadg are important regressors for predicting adg. Further, it was found that sadg interacted with breed whereas dadg did not. What this means is that the way sadg affects adg is different for different breeds but the impact of dadg on adg is (approximately) the same across breeds.

The fitted regression model produces the following expressions that can be used to predict the expected adg for calves of each breed based on sadg and dadg:

```
breed 1: E(adg) = 0.339 + .643 \times sadg + .512 \times dadg
breed 2: E(adg) = 1.242 + .151 \times sadg + .512 \times dadg
breed 3: E(adg) = 2.137 + .207 \times sadg + .512 \times dadg
```

For each breed the coefficient for dadg is 0.512. This means that if sadg is fixed then the estimated value of adg increases by 0.512 for each unit increase in dadg for each breed. In a similar manner the coefficients for sadg can be interpreted as the increase in adg for each unit increase in sadg if dadg is held constant. Note that the coefficients for sadg are different for

each breed. Thus sadg has a the biggest impact on the predicted value of adg for Breed 1 (.643) and the smallest impact for Breed 2 (.151).

Comparing weight gains between breeds is a bit tricky. We need to take into account the levels of sadg and dadg. However, fixing the levels of these two variables at common levels for all three breeds is not reasonable since the ranges of values for sadg and dadg are quite different for the different breeds. For example, the range of sadg is from 1.2 to 2.3 for breed 2 and from 2.6 to 3.9 for breed 3. As an alternative, predictions were made using three scenarios for each breed: (i) a worst case scenario where dadg and sadg are set to their minimum values for that breed, (ii) an average scenario where dadg and sadg are set to their average values for that breed, and a best case scenario where dadg and sadg are set to their maximum values for that breed. Table 1 contains the predicted values for the average adg for each of these situations as along with a 95% confidence interval (an interval that we can be 95% confident will contain the true average adg). From this table it is clear that weight gains are highest for breed 3 and lowest for breed 2.

Breed		sadg	dadg	$\widehat{\mathtt{adg}}$	95% CI
1	min	2.00	1.70	2.50	(2.35, 2.64)
	ave	2.50	2.03	2.99	(2.90, 3.07)
	max	3.00	2.40	3.50	(3.35, 3.64)
2	\min	1.20	1.00	1.94	(1.77, 2.10)
	ave	1.74	1.96	2.51	(2.44, 2.58)
	max	2.30	3.00	3.13	(2.95, 3.30)
3	\min	2.60	2.00	3.70	(3.56, 3.84)
	ave	3.13	2.70	4.17	(4.10, 4.24)
	max	3.90	3.30	4.63	(4.47, 4.80)

Table 1: Predictions of average adg

Statistical Appendix

I started by fitting the regression model that contained all three two-factor interactions in addition to the main effects. The output from the anova command suggested that it was not necessary to retain all three two-factor interactions. I used the added variable F-test to try dropping the two-factor interactions one at a time. The test for dropping dadg:breed gave the highest P-value (0.73) and so I eliminated this term. I then tried eliminating each of the two remaining interactions and found that sadg:dadg could also be dropped (P-value= 0.14). This leaves a model that contains the three main effects and the sadg:breed interaction. An F-test that considers eliminating sadg:breed give a very small P-value (0.004) which means that sadg, breed, and sadg:breed should all be kept. I then tried eliminating the dadg term but this gives an extremely small P-value. Thus I decided to use this model.

The output from summary and dummy.coef for this model is:

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept)
             0.33907
                        0.28834
                                  1.176 0.256809
                                  6.156 1.38e-05 ***
             0.64331
                        0.10450
sadg
breed2
             0.90342
                        0.30171
                                  2.994 0.008580 **
                                  4.968 0.000140 ***
breed3
             1.79835
                        0.36201
dadg
             0.51196
                        0.04318 11.855 2.45e-09 ***
                                 -3.688 0.001992 **
sadg:breed2 -0.49207
                        0.13342
sadg:breed3 -0.43648
                        0.12971
                                 -3.365 0.003941 **
```

0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1 Signif. codes:

Residual standard error: 0.09729 on 16 degrees of freedom Multiple R-Squared: 0.9892, Adjusted R-squared: 0.9852 F-statistic: 244.9 on 6 and 16 DF, p-value: 7.994e-15

> dummy.coef(calf.fit3) Full coefficients are

(Intercept): 0.339073 0.6433073 sadg:

breed: 1 2 3

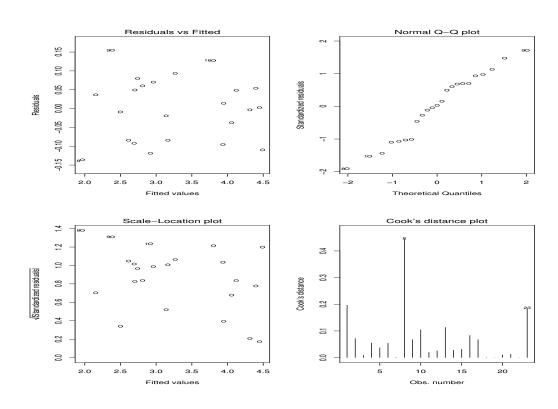
> 0.0000000 0.9034225 1.7983496

0.5119633 dadg:

2 sadg:breed: 3

0.0000000 -0.4920690 -0.4364815

Note that almost 99% of the variability in the response is explained by this model. Diagnostic plots for this model are:



There doesn't seem to be clear evidence of either curvature or a funnel effect in the plot of residuals versus fitted values and the Normal probability plot follows a reasonably straight line. About the only cause for concern is that observation 8 has a somewhat high value of Cook's Distance. I tried deleting this point and re-fitting the model to see what impact this would have on the fitted model. The output from dummy.coef for the fitted model with observation 8 deleted is:

```
> dummy.coef(calf.fit3A)
Full coefficients are
```

(Intercept): 0.4951132 sadg: 0.6266756 breed: 1

: 1 2 3 0.000000 1.047317 1.850831

dadg: 0.4556711

sadg:breed: 1 2 3

0.0000000 -0.5663055 -0.4378921

Although, the fitted coefficients have changed somewhat there is not drastic changed in what the model is indicating about differences between the breeds. Thus I did not discuss the effect of dropping this observation in my report.